

## Some Common Confusions about Hyperbolic Discounting

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- (a) Hyperbolic discounting is not about the discount rate changing over time. A constant discount rate is not essential for time consistency, nor does a varying discount rate create time inconsistency.
- (b) ‘‘Hyperbolic discounting’’ does not, as commonly used, mean discounting using a hyperbolic function.
- (c) Hyperbolic discounting really isn’t about the shape of the discount function anyway.
- (d) Hyperbolic discounting is not about someone being very impatient.
- (e) Hyperbolic discounting is not necessarily about lack of self- control, or irrationality.
- (f) Hyperbolic discounting does not depend delicately on the length of the time period.

$$U_{2008} = C_{2008} + \delta_{2009}C_{2009} + \delta_{2009}\delta_{2010}C_{2010} + \delta_{2009}\delta_{2010}\delta_{2011}C_{2011}. \quad (1)$$

Exponential utility with a constant discount factor  $\delta$  has the form:

$$U_0 = C_0 + \delta C_1 + \delta^2 C_1 + \delta^3 C_2 + \dots, \quad (2)$$

Quasi-hyperbolic utility (also called ‘‘Beta-Delta Utility’’) has the form (with  $0 \leq \beta \leq 1$ ):

$$U_0 = C_0 + \beta\delta C_1 + \beta\delta^2 C_1 + \beta\delta^3 C_2 + \dots \quad (3)$$

The functional form in equation (3) can also be written as:  $U_0 = H * C_0 + \delta C_1 + \delta^2 C_1 + \delta^3 C_2 + \dots$ , where  $H > 0$ , and where  $H > 1$  for a person who distinguishes sharply between current consumption and future consumption. True hyperbolic utility would have the form:

$$U_0 = C_0 + \left(\frac{1}{1+\alpha}\right) C_1 + \left(\frac{1}{1+2\alpha}\right) C_2 + \dots \quad (4)$$

An exponential utility function with the hyperbolic shape can be derived from  $f(1) = \delta_1$ ,  $f(2) = \delta_1\delta_2$ ,  $f(3) = \delta_1\delta_2\delta_3$ , ...  $f(t) = \delta_1\delta_2\delta_3/cdot/cdot/cdot\delta_t$ . so we can calculate  $\delta_t = \frac{f(t)}{f(t-1)}$ , and since  $\delta_t = \frac{1}{1+\rho_t}$ , we can calculate  $\rho_t = \frac{1-\delta_t}{\delta_t}$ .

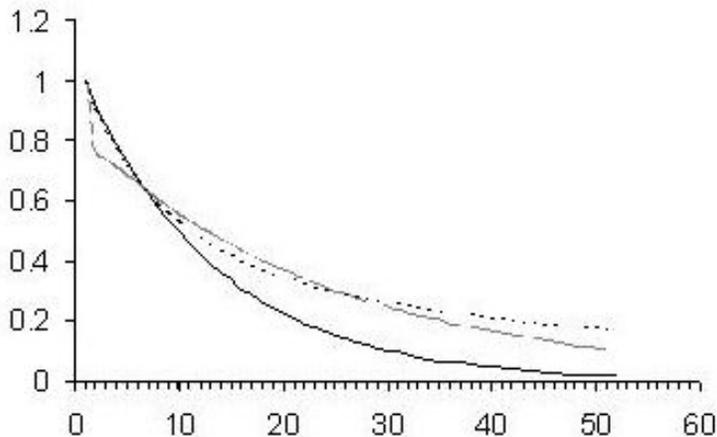


Figure 1:

The Shapes of Exponential (solid), Hyperbolic (dotted), and Quasi-Hyperbolic (dashed) Discounting

$$(\delta_{exp} = .92, f_h(\tau) = \frac{1}{1+.1\tau}, \beta = .8 \text{ or } H = 1.25 \text{ and } \delta_{qh} = .96)$$