11.4 The Informed Player Moves Second: Screening

In <u>screening</u> games, the <u>informed</u> player moves <u>second</u>,
 which means that he moves in response to <u>contracts</u>
 offered by the <u>uninformed</u> player.

✓ An offer conveys <u>no</u> information about the <u>uninformed</u> player.

- ♦ Education V: <u>Screening</u> with a Discrete Signal
 - Players
 - √ a worker and two employers
 - The order of play
 - Nature chooses the worker's <u>ability</u> $a \in \{2, 5.5\}$, the *Low* and *High* ability each having probability 0.5.

The variable a is <u>observed</u> by the worker, but <u>not</u> by the employers.

1 Each employer offers a wage contract w(s).

2 The worker chooses education level $s \in \{0, 1\}$.

3 The worker accepts a contract, or rejects both of them.

4 Output equals *a*.

o Payoffs

$$\sqrt{\pi_{worker}} = w - 8 s/a$$
 if the worker accepts contract $w = 0$ if he rejects both contracts

 $\pi_{employer} = a - w$ for the employer whose contract is accepted 0 for the other employer

♦ The unique equilibrium

• Education V has <u>no</u> pooling equilibrium.

If one employer tried to offer the zero profit <u>pooling</u> contract, w(0) = 3.75, the other employer would offer w(1) = 5.5 and draw away all the <u>Highs</u>.

• Separating Equilibrium 5.1

$$\sqrt{s(Low)} = 0 \qquad s(High) = 1$$

$$w(0) = 2 \qquad w(1) = 5.5$$

- Beliefs do <u>not</u> need to be specified in a screening model.
 - The <u>uninformed</u> player moves first,
 so his <u>beliefs</u> after seeing the moves of the <u>informed</u> player
 are <u>irrelevant</u>.

✓ The <u>informed</u> player is <u>fully</u> informed,
 so his beliefs are <u>not</u> affected by what he observes.

√ This is much like simple adverse selection.

• The modeller does <u>not</u> need to refine perfectness in a screening model.

♦ Education VI: Screening with a Continuous Signal

Players

√ a worker and two employers

• The order of play

Nature chooses the worker's ability $a \in \{2, 5.5\}$, each ability having probability 0.5.

The employers do <u>not</u> observe ability, but the worker <u>does</u>.

1 Each employer offers a wage contract w(s).

The <u>worker</u> chooses <u>education level</u> $s \in [0, 1]$.

3 The worker chooses a contract, or rejects both of them.

4 Output equals *a*.

o Payoffs

$$\sqrt{\pi_{worker}} = w - 8 s/a$$
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- A separating equilibrium
 - Pooling equilibria generally do not exist in screening games 0 with continuous signals, and sometimes separating equilibria in pure strategies do not exist either.

Separating (Nash) Equilibrium 6.1 (with a unique equilibrium path) 0

$$\sqrt{s(Low)} = 0$$
 $s(High) = s^*$

$$w(s) = 2 \qquad \text{if } s < s^*$$

$$5.5 \qquad \text{if } s \ge s^*$$

5.5 if
$$s \geq s^*$$

- ✓ In any <u>separating</u> contract,
 the *Lows* must be paid a wage of 2 for an <u>education</u> of 0,
 because this is the most attractive <u>contract</u> that breaks even.
- ✓ The <u>separating</u> contract for the *High*s must maximize their utility subject to the <u>constraints</u> discussed in Education I.

- √ the participation constraints for the employers
 - $w(0) \le a_L = 2$ and $w(s^*) \le a_H = 5.5$
 - <u>Competition</u> between the employers turns the inequalities into <u>equalities</u>.

the <u>self-selection</u> constraint for the <u>Lows</u>

•
$$U_L(s=0) = w(0) - 0 \ge w(s^*) - 8 s^*/2 = U_L(s=s^*)$$

• This constraint is satisfied as an <u>equality</u> if $s^* = 0.875$, and is true for higher values of s^* .

 \checkmark the <u>self-selection</u> constraint for the <u>Highs</u>

•
$$U_H(s=s^*) = w(s^*) - 8s^*/5.5 \ge w(0) - 0 = U_H(s=0)$$

• This constraint is true, regardless of the value of s^* .

The <u>education level</u> for the *Highs* in Separating Equilibrium 6.1 is <u>unique</u> at 0.875,

because the <u>employers</u> compete to offer the most attractive <u>contract</u> that satisfies the participation and incentive compatibility constraints.

The <u>most</u> attractive is the separating <u>contract</u> that Pareto dominates the other separating contracts by <u>requiring</u> the relatively low separating <u>signal</u> of $s^* = 0.875$. • <u>Competition</u> in offering attractive contracts rules out <u>pooling</u> contracts.

The <u>nonpooling</u> constraint,required by competition between the employers, is

•
$$U_H(s = s^*) = w(s^*) - 8 s^*/5.5 \ge U_H(pooling).$$

The <u>nonpooling</u> constraint is satisfied even with the most attractive possible <u>pooling</u> contract, which leads to $U_H(pooling) = 3.75$.