# "Why Firms Reduce Business Risk Revisited: Projects with Risky Cash Flows Are Harder To Evaluate?"

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#### Abstract

Firms care a lot about "risk management": the practice of hedging risks— whether they are correlated with market risk or not. The standard reasons why widely held corporations might be averse to idiosyncratic risk are principal-agent problems, bankruptcy costs, external finance, and tax convexity. This paper offers a different reason: risk makes business decisions more difficult. We must distinguish, however, between risk over the expected value of profits ("value risk") and risk over the volatility of cash flows ("cash-flow noise"). Value risk is good because an unprofitable policy can be abandoned (option value). Cash-flow noise is bad because it makes learning when to abandon more difficult. This distinction is unrelated to Knightian risk or ambiguity aversion, and it matters even if the firm's agents are risk neutral.

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#### 1. INTRODUCTION

Risk is commonly divided into two categories: systematic and idiosyncratic. A company's systematic risk is the part of its risk correlated with the returns an investor could earn by holding other assets in the economy; its idiosyncratic risk, the part which is not. Under the CAPM and other theories of asset pricing a publicly traded corporation should be averse to systematic but not idiosyncratic risk because its shareholders can diversify away idiosyncratic risk by holding a variety of assets. Thus, firms should not take idiosyncratic risk into consideration.

Yet it seems firms do avoid idiosyncratic risk in both investment (Panousi & Papanikolaou, [2012]) and operating decisions ((Amit & Wernerfelt [1990], Chatterjee, Lubatkin & Schulze [1999]). They manage enterprise risk (Bromiley, McShane, Nair & Rustambeko [2015]), hedge against movements in commodity prices and currencies (Stulz [1996], Smith [2008]), smooth accounting earnings (Burgstahler & Dichev [1997]), and buy insurance (Harrington, Niehaus & Risko [2002]). There may even be a "diversification discount": investors prefer firms with diversified lines of business (Villalonga [2004], though see also Laevena & Levine [2007]).

The most common explanation for aversion to idiosyncratic risk is that to incentivize managers the firm must link pay to firm-specific performance. As a result, managers wish to reduce risk regardless of shareholder desires. Even if shareholders can control the managers they will need to design complex contracts and pay extra for bearing risk (Smith [2008] Panousi & Papanikolaou, [2012], Glover & Levine [2017]). A second explanation is bankruptcy costs. Bankruptcy arises even from idiosyncratic risk and creates not just direct costs in reorganization but indirect costs because of anticipatory moves of lenders, suppliers, and customers (Stulz [1996], Kuerstein & Linde 2017]). A third explanation is that external finance is more costly than retained earnings as a source of capital. If retained earnings are variable, the firm will sometimes be short of capital and sometimes have more than it has use for (Froot, Scharfstein & Stein [1993]). A final explanation is convex taxation, which makes it advantageous to smooth profits (Nance, Smith & Smithson [1993]).

This article offers a different explanation, one that does not seem to have been discussed despite its common sense: risk's effect on the quality of decisions. If the firm encounters more noise in evaluating whether an activity is profitable or not, it will make worse decisions, so it chooses to avoid risk.

The value of risk has indeed been much studied in the context of decisions, in the theory of real options, but with the opposite conclusion: risk is good, because option value increases with volatility. If an activity might have either high or low returns, the firm has the option to abandon if the return turns out to be low. This suggests that corporations should be risk-loving, not risk-averse. Real options have been the topic of much study, some focussed on adjustment costs and competitive conditions (Hartman [1972], Abel [1983], Kim & Kung [2017]), some on valuation (Dixit & Pindyck [1994], Trigeorgis [1996], Lambrecht [2017]), and some on management implications (Trigeorgis & Reuer [2017]).

The downside— this paper's point— is that volatility makes learning more difficult. Idiosyncratic risk hurts learning even more than systematic risk, since it cannot be backed out from the market return. Thus, two contrary forces are at work in volatility: the advantage of a more valuable option, and the disadvantage of not knowing what to do with it. I propose distinguishing between "value risk" and "cashflow noise". Value risk increases with divergence in possible expected values. Cash-flow noise increases with the variability of cash flows, for given expected value. Value risk has positive option value because the firm has the option to discontinue the policy if it learns the expected value is low. Cash-flow noise hurts option value because it hinders the firm from knowing whether to exercise the option. Thus, when firms avoid projects whose idiosyncratic risk consists of cash-flow noise, they are being rational even if their investors are risk-neutral.

#### 2. Distinguishing Value Risk from Cash-flow Noise

There are two reasons one might say, "This project is risky." The first is that one doesn't know whether the project is profitable. The second is that even though profitability is known, the cash flow varies over time. Profitability is akin to Aristotle's "substance", a data-generating process, with cash flows as the data (Aristotle's "accidents"). We will call dispersion in possible expected values "value risk", and dispersion in cash flows around the expected value "cash-flow noise".

More formally, let activity A have the realized cash flows  $X_{it}^A$ ,  $t = 1, \ldots, T$  given by the stationary stochastic process  $X_i^A$ ,  $i = 1, \ldots, N^A$  with probabilities  $F_i^A$  given by distribution  $F^A$ . An example for  $t = 1, \ldots, 10$ , is that either  $X_t = X_{1t}^A = 10$  with probability .7 and 0 with probability .3 for all t, or  $X_t = X_{2t}^A = -100$  with probability .6 and 0 with probability .4 for all t, where  $F_1^A = .9$  and  $F_2^A = .1$ . Then  $E(X_1^A) = 7, E(X_2^A) = -60$ , and  $E(X^A) = .9(7) + .1(-60) = 0.3$ .

Following the standard partial ordering of riskiness in Rothschild & Stiglitz (1970), we will say that when  $E(X^A) = E(X^B)$ , activity A has greater value risk than B if any agent with strictly concave utility would prefer  $\{E(X_i^B), F^B\}$  to  $\{E(X_i^A), F^A\}$ . We will say that A has greater cash flow noise than B if any agent with strictly concave utility would prefer  $\{X_i^B - E(X_i^B), F_i^B\}$ ,  $i = 1, \ldots N^B$  to  $\{X_i^A - E(X_i^A), F_i^A\}$ ,  $i = 1, \ldots N^A$ .

Confusing the two kinds of risk is easy because we model them the same way. Suppose project X has 70% chance of yielding a cash flow of +1 and 30% chance of 0 in any particular year, whereas project Y has 70% chance of yielding a steady cash flow of +1 and 30% chance of 0. They each have an annual expected value of .7, but project X has zero value risk and project Y has zero cash flow noise.

#### Example 1: A Firm Choosing Which Product to Sell

A firm is considering which of several new brands of soap to introduce for a three-year product cycle, after which the brand will be replaced by something else. Assume zero time discounting. The firm, which is either "well-suited" or "ill-suited" to sell this particular product with probability .5 of each, does not know its ability. Market conditions will be "normal" in some years and "difficult" in others. Product A is the safest, with no risk whatsoever. Product B's value is unknown, but its cash flow will not depend on market conditions. Product C is the most complicated, yielding positive profit in normal years and losses in difficult years. Specifically:

Product A yields a yearly cash flow of 0, regardless of market conditions or whether the firm is well-suited.

Product B yields a yearly cash flow of +1 if the firm is well-suited and -1 if ill-suited, regardless of market conditions. Product B's expected cash flow is also 0.

Product C yields a cash flow of +2 in a normal year, which has 70% probability. If the firm is well-suited, it yields a cash flow of -4/3 in a difficult year, for an expected yearly cash flow of +1 over all years. If the firm is ill-suited, it yields a cash flow of -8 in a difficult year, for an expected flow of -1. Product C's overall expected cash flow is also 0.

If the firm chooses Product A, it has no decisions to make and the product's lifetime value is 0.

If the firm chooses Product B, it will immediately discover if it is illsuited because the cash flow will be -1 the first year, and it will cancel the product. The expected three-year profit consists of a 50% chance of -1+0+0 and a 50% chance of +1+1+1, for an expected profit of +1, even though if the firm refused to cancel the expected value would be 0.

If the firm chooses Product C, the best strategy is to keep selling until a year in which the cash flow is -8, which would make plain that it is ill-suited to sell soap, and then cancel. If the firm is ill-suited, its probability of selling for one year would be .30, .21 for two years, and .49 for three years, (which includes probability .34 of never discovering the truth), for an expected profit of -2.19. If the firm is well-suited, its expected three-year profit is +3. Overall, expected profit is  $.405.^{1}$  Product C is better than Product A, because it has option value, but worse than B, because learning C's value is more difficult.<sup>2</sup>

In Example 1, value risk is desirable. Product B's uncertainty makes it superior to Product A— but only because the firm both (a) learns, and (b) has the option to cancel the product. Product C has even more uncertainty than B, but the wrong kind: cash-flow noise. That uncertainty does not affect option value directly, because the firm has the same option to cancel an unprofitable product. Indirectly, however, cash-flow noise makes learning more expensive: it costs .5(-1) to learn that product B is unprofitable, compared to .5(-2.19) for product C.

Example 1 is reminiscient of ambiguity aversion, the Ellsberg Paradox's idea that even if two lotteries have the same risk, if one of them is a "lottery of lotteries" people will avoid it (Ellsberg [1961], Ju & Miao [2012]). Product C is indeed a lottery of lotteries, a 50-50 gamble between two different 70-30 lotteries rather than a 50-50 gamble between two integers, like product B. As with the Ellsberg Paradox, easier decisionmaking is preferred. An executive viewing an MBA's powerpoint proposal to undertake product C might well worry about the cognitive cost of calculating the value of complex lotteries, the likelihood of making a mistake, and the danger of being fooled. Here, what is driving his distaste for C is that it requires more expensive experimentation. This will be apparent in the next section's model, in which the two alternatives are equally simple, with cash flow distributions that differ only in a single parameter.

 $<sup>{}^{1}.405 = .5[.3(-8) + .21(2 - 8) + .147(4 - 8) + .343(6)] + .5[3].</sup>$ 

<sup>&</sup>lt;sup>2</sup>Whether the firm can switch products in the middle of the three-year product life cycle does not matter. Even with switching, if product C is chosen and the firm then discovers it was ill-suited the first year, C would be discontinued, but B would be no more profitable for the ill-suited firm.

#### 3. A Continuous-Time Model

This section's model will use stochastic calculus, a tool often used to look at adoption and abandonment decisions (see Pindyck [1993], Dixit & Pindyck 1994, p. 345], Bernardo & Chowdhry [2002], Decamps , Mariotti & Villeneuve [2006], Kwon & Lippman [2011]). The model makes no claims to technical novelty; indeed, it could be considered a special case of Lippman & Ryan (2003), despite its different look.<sup>3</sup> It will, however, be useful for thinking about the difference between value risk and cash-flow noise.

Consider a single project whose type  $\theta \in \{H, L\}$  is initially unknown, drawn from a prior distribution with  $Pr(\theta = H) = p_0 \in (0, 1)$ . The project delivers a stochastic cash flow  $X_t$  according to a continuous-time diffusion process:

$$dX_t = \mu(\theta)dt + \sigma dW_t, \tag{1}$$

where  $W_t$  is a standard Brownian motion process for positive mean  $\mu(\theta)$  and standard deviation  $\sigma$ . Let the possible means of the process be  $\mu(H) = \pi$  and  $\mu(L) = -\pi$ . The firm discounts cash flows at rate r. Its only decision, which it makes every instant, is whether to continue the project or abandon it.

Here the parameter  $\mu(\theta)$  represents the amount of value risk and  $\sigma$  the amount of cash-flow noise. As time passes, the firm continuously updates its posterior belief  $p_t$  about  $\mu(\theta)$  using Bayes's rule. Rather than analyzing the cash flow path,  $X_t$ , it is most convenient (see section 2.3 of Daley & Green [2012] or section A1 of Kolb [2019]) to analyze the belief path,  $p_t$ , converting to log-likelihood beliefs,  $Z_t$  that update linearly and vary on  $[-\infty, +\infty]$  as  $p_t$  varies on [0,1]:

$$Z_t \equiv \ln\left(\frac{p_t}{1-p_t}\right) \tag{2}$$

<sup>&</sup>lt;sup>3</sup>Lippman & Ryan (2003) uses  $\mu(H)$  and  $-\mu(L)$  rather than  $\pi$  and  $-\pi$ . Imposing symmetry makes my propositions simpler and stronger (because less general), and allows value risk to be parameterized by  $\pi$ . An even earlier and more general analysis of the project stopping problem is Karatzas (1984).

Using filtration results standard in the literature (e.g., section 3) of Bolton & Harris [1999]), the law of motion for the posterior belief conditional on the type being  $\theta \in \{H, L\}$  is

$$Z_t^H = \frac{\phi^2}{2}dt + \phi dW_t \tag{3}$$

$$Z_t^L = -\frac{\phi^2}{2}dt + \phi dW_t, \qquad (4)$$

where  $\phi \equiv \frac{\mu(H) - \mu(L)}{\sigma} = \frac{2\pi}{\sigma}$ .

The firm's optimal strategy is to abandon the project whenever the belief  $Z_t$  falls to some lower threshold  $z^*$ , as stated in the following proposition.

**Proposition 1.** The firm's optimal abandonment threshold is
$$z^* = \ln\left[\frac{\pi^2 + r\sigma^2 - \pi\sqrt{\pi^2 + 2r\sigma^2}}{r\sigma^2}\right] < 0, \quad (5)$$
and its value function is

an

$$V(z) = \begin{cases} \left(\frac{e^{z}-1}{e^{z}+1}\right)\frac{\pi}{r} + \left(\left(\frac{1-e^{z^{*}}}{e^{z}+1}\right)e^{m(z-z^{*})}\right)\frac{\pi}{r} & \text{if } z \ge z^{*} \\ 0 & \text{otherwise,} \end{cases}$$
(6)  
where  $m = \frac{1}{2} - \sqrt{\frac{1}{4} + \frac{r\sigma^{2}}{2\pi^{2}}} < 0.$ 

*Proof.* By Ito's Lemma, since the expected flow return is  $p_t \pi + (1 - p_t) \pi + (1$  $p_t(-\pi) = \left(\frac{e^z-1}{e^z+1}\right)\pi$ , the value function prior to abandonment satisfies

$$rV(z) = \left(\frac{e^z - 1}{e^z + 1}\right)\pi + \left(\frac{e^z - 1}{e^z + 1}\right)\frac{2\pi^2}{\sigma^2}V'(z) + \left(\frac{2\pi^2}{\sigma^2}\right)V''(z).$$
 (7)

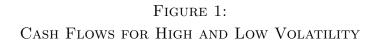
This differential equation has solutions of the form

$$V(z) = \left(\frac{e^{z} - 1}{e^{z} + 1}\right) \frac{\pi}{r} + \left(\frac{e^{mz}}{e^{z} + 1}\right) C_{1} + \left(\frac{e^{(1-m)z}}{e^{z} + 1}\right) C_{2}, \qquad (8)$$

where m is defined in the proposition and we need to find  $C_1$  and  $C_2$ . We know that the value is  $\frac{\pi}{r}$  if the project type is high, which is belief  $p_t = 1$  (and thus  $Z_t = ln\left(\frac{p_t}{1-p_t}\right) \to \infty$ ), so it must be true that  $\lim_{z\to+\infty} V(z) = \frac{\pi}{r}$  and we can conclude that  $C_2 = 0$ . Pinning down  $z^*$  and  $C_1 = \frac{\pi}{r} (1 - e^{z^*}) e^{-mz^*}$  then follows from the standard value matching and smooth pasting conditions  $V(z^*) = 0$  and  $V'(z^*) = 0$  (Dixit [1993]). Simplifying the second term yields (6).

Figures 1 and 2 show one realization of stochastic process paths over time when r = .12, the project is unprofitable ( $\mu(\theta) = -15$ ), and the belief starts at 40% probability the project is profitable.<sup>4</sup> The red paths are for  $\sigma = 10$  and the blue paths for  $\sigma = 30$ , using the same discrete approximation realization of the Weiner process  $dW_t$  for both. The optimal thresholds  $p^*(\sigma)$  are .02 and .14, which are below .50 because of option value. With low volatility, the belief that the project is high must fall all the way to 2% before abandonment, but the information is so good that this happens quickly, in period 299, after losses have only accumulated to 11. With high volatility, the belief only needs to fall to 35%, but the information is poor enough that this happens in period 800, after losses have accumulated to 42.

<sup>&</sup>lt;sup>4</sup>The Python 3 code is available at http://rasmusen.org/papers/risk\_aversion.py.



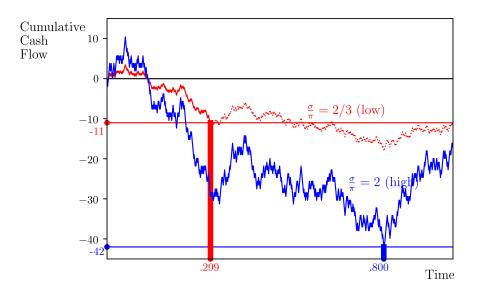
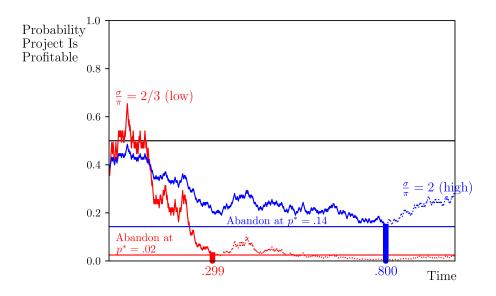


FIGURE 2: Beliefs for for High and Low Volatility



Returning to the optimal value function, equation (6), note that it is composed of two terms. The first term represents the expected value of running the project forever,  $(2p_t-1)\left(\frac{\pi}{r}\right)$ , since  $\frac{e^{z_t}-1}{e^{z_t}+1} = 2p_t - 1$ . That term is positive if  $p_1 > 0$  and negative if  $p_t < 0$ . The second term represents the gain from the ability to abandon the project after poor returns. It is always positive, because  $z^* < 0$  so  $1 - e^{z^*} > 0$ . If  $z_t = z^*$ , then  $\frac{1-e^{z^*}}{e^{z^*+1}} = 2p^* - 1$  and  $e^{m(z_t-z^*)} = 1$ , so the second term's magnitude is exactly equal to the first term's. The value to running the project another instant is  $rV(z_t)$ , so when  $z_t = z^*$ , the positive learning flow from continuing is exactly cancelled by the negative cash flow. This, of course, is what we used in solving the V(z) function, because for any lower  $z_t$  the option value would not be worth the cash flow loss. The next proposition shows how value risk and cash-flow noise affect the tradeoffs.

**Proposition 2.** As cash-flow noise  $\sigma$  rises, the abandonment threshold  $v^*$  increases and the project's value falls. As value risk  $\pi$  rises, the abandonment threshold decreases and the project's value rises.

*Proof.* In what follows, we use  $C_1 = \frac{\pi}{r} (1 - e^{z^*}) e^{-mz^*}$  from Proposition 1's proof so we can write the positive part of the value function as

$$V^{+}(z) = \left(\frac{e^{z} - 1}{e^{z} + 1}\right) \frac{\pi}{r} + \left(\frac{e^{mz}}{e^{z} + 1}\right) C_{1}$$
(9)

We will define F(z) to be the function which extends  $V^+(z)$  over the entire real line. From Proposition 1's proof,  $V(z^*) = 0$  and  $V'(z^*) = 0$ , and V(z) > 0 for large enough z, so since  $F(z)(e^z + 1)$  is an exponential polynomial with at most two sign changes it follows that F(z) is nonnegative with a single minimum at  $z = z^*$ .

First, consider the effect of an increase from  $\sigma$  to  $\tilde{\sigma}$  and let tilde denote the solution components for  $\tilde{\sigma}$ . We claim that F(z) and  $\tilde{F}(z)$ can intersect at most once, since  $\Delta(z) = (e^z + 1)[\tilde{F}(z) - F(z)] =$  $\tilde{C}_1 e^{\tilde{m}z} - C_1 e^{mz}$ , where the expression in brackets is an exponential polynomial with exactly one sign change. Now  $\frac{\partial z^*}{\partial \sigma} = \frac{2\pi}{\sigma \sqrt{\pi^2 + 2r\sigma^2}} > 0$ , so  $\tilde{z}^* > z^*$ . The minimum of  $\tilde{F}(z)$ , but not of F(z), is at  $\tilde{z}^*$ , so  $\tilde{F}(\tilde{z}^*) = 0, F(\tilde{z}^*) > 0$ , and  $\Delta(z^*) < 0$ . Since  $\Delta(z^*) > 0$  by the same kind of argument, there exists a root  $\hat{z} \in (z^*, \tilde{z^*})$  of  $\Delta(z)$  where  $\Delta(\hat{z}) = 0$  and  $\tilde{F}$  intersects F from above. Since that is the only sign change  $\Delta(z)$  can have, it follows that that  $F(z) > \tilde{F}(z)$  for  $z > \hat{z} < \tilde{z}^*$ . Recall that V(z) is identical to F(z) except for equalling zero on  $z < z^*$ . Hence,  $\tilde{V}(z) = 0$  for all  $z < \hat{z} < \tilde{z}^*$ , so  $V(z) > \tilde{V}(z)$  for all  $z > z^*$  (and  $V(z) = \tilde{V}(z) = 0$  for  $z \le z^*$ ).

Next, consider the effect of an increase from  $\pi$  to  $\tilde{\pi}$ , and use tilde to denote solution components for  $\tilde{\pi}$ . We have  $\Delta(z) = (e^z + 1)[\tilde{F}(z) - F(z)] = \frac{\tilde{m}-m}{r}(e^z-1)+\tilde{C}_1e^{\tilde{m}z}-C_1e^{mz}$ . Now  $\frac{\partial z^*}{\partial \pi} = -\frac{2}{\sqrt{\pi^2+2r\sigma^2}}$ , so  $\tilde{z}^* < z^*$ , and thus  $\Delta$  has a root in  $(\tilde{z}^*, z^*)$  where  $\Delta$  crosses 0 from below. We claim that any root above  $\tilde{z}^*$  must cross from below, and thus there is only one root above  $\tilde{z}^*$ . Note that if z is a root, then  $\tilde{F}(z) = F(z)$ , so  $\Delta'(z) = \Delta'(z) - \tilde{m}\Delta(z) = \frac{\tilde{m}-m}{r} [e^z - \tilde{m}(e^z - 1)] + C_1 e^{mz}(\tilde{m} - m)$ . It is easy to verify that  $\tilde{z}^* = \ln \frac{-\tilde{m}}{1-\tilde{m}}$ , so the first term is positive for all  $z > \tilde{z}^*$ . The second term is always positive because m increases in  $\pi$ , so the claim holds. It follows that for all  $z \ge z^*$ , we have  $\Delta(z) =$  $\tilde{F}(z) - F(z) > 0$ . Moreover, for  $z \le \tilde{z}^*$ ,  $\tilde{V}(z) = V(z) = 0$  and for  $z \in (\tilde{z}^*, z^*)$ ,  $\tilde{V}(z) > 0 = V(z^*)$ . We conclude that  $\tilde{V}(z) \ge V(z)$  for all  $z \in \mathbb{R}$ , with strict inequality for all  $z > \tilde{z}^*$ .

The firm's belief about project type changes faster if  $\pi$  is big and  $\sigma$  is small. This is equivalent to faster learning as news comes in from the cash flows. A bigger  $\sigma$  means bigger movements in cash flows, a more variable cash flow process, but when converted to belief space it means smaller movements in beliefs, because a given change in cash flow is less communicative of whether the state is high or low. As the cash-flow noise  $\sigma$  increases, the signal-to-noise ratio of the cash flow signal decreases, and the firm learns more slowly about the project's type. This reduces the option value to continuing the project to try to learn more, which is the second term in the value function. When the option value falls, that makes the firm worse off and causes it to

abandon projects sooner. Thus, the firm should be averse to cashflow noise because it makes decisionmaking harder, whether or not its managers and shareholders are risk-averse in their utility functions.

On the other hand, when value risk increases the spread between the expected returns  $-\pi$  and  $\pi$  of low and high projects, the firm benefits twofold. First, the upside potential  $\pi/r$  from running a good project forever increases, while the downside potential is still bounded below at zero, as the firm can always abandon it. This is the standard result that increasing variance increases an option's value. This first benefit would apply even if the firm's learning was instantaneous as in Example 1. The second benefit is that the signal-to-noise ratio increases and the firm can more quickly learn about the project's type. The firm can respond with more aggressive experimentation. Its abandonment threshold is lower because it is willing to continue the project even under a pessimistic belief because quicker learning means quicker abandonment if the project type is indeed low.

We have described the model as one of project choice, but it could apply to any of a business's activities. In this setting of normally distributed risk, we can also interpret a higher value of  $\sigma$  as the result of adding normally distributed zero-mean noise to an existing activity, since adding an independent zero mean normal variable to an existing normal variable increases the variance while leaving normality and the mean unchanged. In particular, one could view accounting systems as attempts to reduce cash-flow noise. In practice, standard business earnings are not cash flows, which are higher-variance measures of profitability, but flows of accruals and depreciation, which require careful definition intended to balance current economic profits against variability across time that makes determining profitability more difficult. Thus, we can view accounting imperfections as a source of risk in "cash flows". Deficiencies in accounting quality would often merely be idiosyncratic risk, but it is risk that hurts the quality of investment decisions.

# 4. Two Distractions: Knightian Uncertainty and the Principal-Agent Problem

Splitting risk into two types brings to mind Knight's distinction between risk and uncertainty (Knight [1921]). What Knight was getting at remains controversial (see Leroy & Singell [1987]), but one interpretation is that Knightian risk is unpredictability with known probabilities in repeated situations, the kind of risk that is insurable, whereas Knightian uncertainty is unpredictability in one-time situations where the probabilities are more subjective. In Example 1, the cash-flow noise was about whether the market was normal or difficult, something objective that would seem to be Knightian risk. The value risk was that the firm might be either well-suited or ill-suited, something "unknowable" even though the firm will have subjective probabilities, and would thus be Knightian uncertainty. Similarly, in the continuous-time model, the cash flows were Knightian risk, but the expected value was either high or low, but unknown: Knightian uncertainty. Example 2 will illustrate that this is not a reliable equivalence.

## Example 2: Hedging Foreign Exchange Risk

An American firm has set up a London office for a three-year period. The new office is a "good" or "bad" idea with equal probability. The office buys and sells in both dollars and pounds, so it is unclear how the exchange rate affects its profitability. If the office is a good idea, though, the profit will be +1 if the exchange rate moves beneficially, which has probability .70, and 0 if it moves harmfully, an expected annual profit of +.7. If the office is a bad idea, the profits will be 0 or -1, an expected profit of -.3. The firm's optimal strategy is to open the office, and shut it down if and only if its profit is seen to be -1 in some year. If the idea is a good one, the expected profit will then be 2.1. If the idea is a bad one, the office will have 30% probability of closing after one year, 21% after two years, 14.7% after three years due to losses in the third year, and 34.3% of operating profitably for three years and closing down only because the three-year period is over. Its expected profit if the idea is bad is -.657. Overall, balancing the

probability the idea is good with that it is bad, the expected profit is .7215.<sup>5</sup>

Now suppose the firm instructs the office to hedge its foreign exchange risk. If the office is a good idea and hedging is costless, its profit each year is +.7, while if it is a bad idea, its profit each year is -.3. The firm will know to shut down the first year if its profit is -.3, so the expected profit over the three years is .5(-.3) + .5(.7+.7+.7) = .90. This is higher than .7215, so the hedging helps, and the firm would be willing to pay as much as .1785 in transactions costs to be able to hedge.

As in Example 2 and the continuous-time model, the exchange rate risk is insurable and objective, so it would seem that again cash-flow noise corresponds to Knightian risk. Whether the London office is a good idea or not appears to be subjective and uninsurable, so value risk would correspond to Knightian uncertainty. Knightian uncertainty would thus be good for profit, and Knightian risk would be bad.

But Example 2 can be interpreted to give the opposite results. Suppose the firm has extensive experience setting up foreign offices, and has found that in exactly 50% of them the idea is a good one. Then the value risk is Knightian risk. Moreover, while exchange rate risk is insurable, the big problem is that the firm doesn't know enough about the inner workings of the office to know whether it benefits from a strong dollar or a weak one. Thus, the cash-flow noise is Knightian uncertainty. The questions of whether (a) there is opportunity for learning because of value risk, and (b) whether learning will be difficult because of cash-flow noise are separate from whether the probabilities are subjective or objective.

 $<sup>^{5}</sup>$ Another strategy is to close down the London office the first year if -1 is observed, or the second year if 0 is observed in the first year and -1 or 0 in the second. That would have expected profit of -.51 if the idea is bad, of -.51 and 1.547 if it is good, an average of .5185.

For our last example, we will return to the principal-agent problem. I have emphasized that option learning is an alternative to managerial risk aversion as an explanation for corporate aversion to idiosyncratic risk. It is also, however, a supplement to the principal-agent explanation, a supplement that applies even if the agent is risk-neutral. That noise worsens a principal-agent problem is an old idea. Holmstrom's classic 1979 "sufficient statistic" paper notes how the informativeness of a signal is hurt by additional risk, and the negative welfare effect shows up naturally in many models, despite the lack of attention to the implications for corporate decisions. (An exception is D. Hirshleifer & Suh [1992], in which a firm avoids high-variance projects because of the difficulty of incentivizing the manager.) Our next example will be of the problem of incentivizing a risk-neutral manager, to show that option learning does not depend on anyone having concave preferences.

**Example 3: The Principal-Agent Problem**. Management is considering one of two protocols for managing customers. Under Protocol X, the worker dealing with a customer reads from a script. If the worker exerts high effort, the customer is satisfied, a value of +10 for the firm. If he exerts low effort, the customer is dissatisfied, a value of -10. Under Protocol Y, the worker is trained to try to adapt to the particular customer. If the worker exerts high effort, the customer is highly satisfied with probability .5, a value of +40 for the firm and dissatisfied with probability .5, a value of -20, which comes to an expected value of +10. If he exerts low effort, the customer is satisfied with probability 1/6 and dissatisfied with probability 5/6, which comes to an expected value of w - e for wage w and effort e = 0 or 3, and their expected utility must equal at least 1 to take the job. They cannot be paid a negative wage.

First let us look at the optimal contract for Protocol X. If the company pays the worker 4 if the customer is satisfied and 0 otherwise, the worker would have utility of 1 (= 4 - 3) from high effort and 0 from low effort and so would choose high effort. With the contract

 $(w_{sat} = 4, w_{diss} = 0)$ , the firm ends up obtaining +10 from the customer and paying 4 to the worker.

Protocol Y takes a bit more consideration. The participation constraint is  $E(w - e | high effort) = .5w_{sat} + .5w_{diss} - 3 \ge 1$ . The incentive compatibility constraint is  $E(w - e|high \ effort) \geq E(w - e|high \ effort)$  $e|low \ effort)$ , which is  $.5w_{sat} + .5w_{diss} - 3 \ge (1/6)w_{sat} + (5/6)w_{diss} - 0$ . Because the wage cannot be negative, the biggest gap between  $w_{sat}$ and  $w_{diss}$  is if  $w_{diss} = 0$ , so the optimal contract will choose that. The participation constraint then requires  $.5w_{sat} + .5(0) - 3 \ge 1$ : the worker is willing to take the job if the contract is  $(w_{sat} = 8, w_{diss} = 0)$ . But the incentive compatibility constraint tells us that  $.5w_{sat} + .5(0) - 3 \ge$  $(1/6)w_{sat} + (5/6)(0) - 0$ : the lowest  $w_{sat}$  that will induce high effort is  $w_{sat} = 9$ . As a result, the firm will wish to use an "efficiency wage", a contract that gives the worker more than his reservation utility because the firm needs to be generous to induce effort (Yellen [1984], Rasmusen [2007 ch. 8]). With the contract  $(w_{sat} = 9, w_{diss} = 0)$ , the firm would end up obtaining an expected value of +10 from the customer and paying an expected wage of 4.5 to the worker. So Protocol Y is worse, with a profit of 5.5 instead of 6.0.

What Example 3 illustrates is that even if both employer and employees are risk-neutral, risk in cash flows creates contracting costs. The basic idea in principal-agent models is that if agents are riskaverse then when output is noisy the optimal contract balances the incentivizing effect of incentive pay against the extra risk that requires a higher expected wage. In Example 3, the agent needs no compensation for bearing risk, since he is risk-neutral, but noisy output requires divergence in pay to incentivize effort. When pay is bounded below by zero, the firm needs to increase the upper bound and thus the expected value, of pay.

#### 5. Concluding Remarks

What's wrong with risk? Our usual answer is concavity of utility: sometimes you have too much, sometimes too little. We focus so much on utility that we neglect another answer: Risk makes it hard to figure out what to do. On retiring to the family farm, my parents hung up a sign on the front porch saying "Simplify". Executives live a frenzied existence. Much of their job is to solve unexpected problems. leaving less time than they would like for evaluating people and projects. They want simplicity, and if they can get a steady bottom-line, whether positive or negative, that simplifies their decisionmaking.



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